SB/ SX

KVPY QUESTION PAPER – STREAM SB/SX NOVEMBER 1, 2015

# One-Mark Questions

# MATHEMATICS

satisfy the simultaneous equations The number of ordered pairs (x, y) of real numbers that

$$x + y^2 = x^2 + y = 12$$

D.

2 If z is a complex number satisfying  $|z^3 + z^{-3}| \le 2$ , then the maximum possible value of  $|z+z^{-1}|$  is

 $2\sqrt{2}$ 

D.

- 10072

 $2014^3 - 2013^3 + 2012^3 - 2011^3 + \dots + 2^3 - 1^3$  is

largest perfect square that

divides

- D. 20142

4. Suppose OABC is a rectangle in the xy-plane where O is the origin and A, B lie on the parabola  $y = x^2$ . Then C must lie on the curve

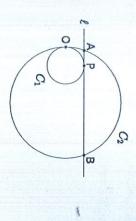
$$y = x^2 + 2$$

$$y = 2x^2 + 1$$

$$y = -x^2 + 2$$

D. 
$$y = -2x^2 + 1$$

5. Circles  $C_1$  and  $C_2$ , of radii r and R respectively, touch each other as shown in the figure. The line  $\ell$ , which is parallel to the line joining the centres of  $C_1$  and  $C_2$ , is tangent to  $C_1$  at P and intersects  $C_2$  at A,B. If  $R^2 = 2r^2$ , then  $\angle AOB$  equals



A. 
$$22\frac{1}{2}^{\circ}$$

D.  $67\frac{1}{2}^{\circ}$ 

6. The shortest distance from the origin to a variable point on the sphere  $(x-2)^2 + (y-3)^2 + (z-6)^2 = 1$  is

7. The number of real numbers  $\lambda$  for which the equality

$$\frac{\sin(\lambda\alpha)}{\sin\alpha} - \frac{\cos(\lambda\alpha)}{\cos\alpha} = \lambda - 1,$$

holds for all real  $\alpha$  which are not integral multiples of  $\pi/2$  is

00

Suppose ABCDEF is a hexagon such that AB = BC = CD = 1 and DE = EF = FA = 2. If the vertices A, B, C, D, E, F are concyclic, the radius of the circle passing through them is

A. 
$$\sqrt{\frac{5}{2}}$$
B.  $\sqrt{\frac{7}{3}}$ 
 $\sqrt{\frac{11}{5}}$ 
D.  $\sqrt{2}$ 

9. Let p(x) be a polynomial such that  $p(x) - p'(x) = x^n$ , where n is a positive integer. Then p(0) equals

$$n!$$
 B.  $(n-1)!$   $\frac{1}{n!}$  D.  $\frac{1}{(n-1)!}$ 

10. The value of the limit

14.

Let x>0 be a fixed real number. Then the integral

 $|e^{-t}|x-t|dt$  is equal to

$$\lim_{x \to 0} \left( \frac{x}{\sin x} \right)^{6/x^2}$$

- e-1/6
- 11. Among all sectors of a fixed perimeter, choose the one sector (i.e., the angle between the bounding radii) is with maximum area. Then the angle at the center of this

- B
- D.
- 12. Define a function  $f: \mathbb{R} \to \mathbb{R}$  by

$$f(x) = \max\{|x|, |x-1|, ..., |x-2n|\},\,$$

where n is a fixed natural number. Then  $\int f(x)dx$  is

- ₩.
- 3n
- D.
- If p(x) is a cubic polynomial with p(1)=3, p(0)=2

13.

- CA

and p(-1) = 4, then  $\int p(x) dx$  is

- D.B.

- An urn contains marbles of four colours: red, white, blue A.  $x + 2e^{-x} - 1$  $x + 2e^{-x} + 1$ D. **B**.  $-x-2e^{-x}+1$  $x - 2e^{-x} + 1$
- 15. replacement, the following events are equally likely: and green. When four marbles are drawn without
- the selection of four red marbles;
- the selection of one white and three red marbles;
- the selection of one white, one blue and two red
- the selection of one marble of each colour

condition is The smallest total number of marbles satisfying the given

- 19
- B. 21
- D. 69
- 16. one ball? n trials, what is the probability that  $B_1$  contains at most shows k, then j balls are put into the box  $B_k$ . After two fair dice  $D_1$ ,  $D_2$  are thrown. If  $D_1$  shows j and  $D_2$ There are 6 boxes labelled  $B_1, B_2, ..., B_6$ . In each trial,

A. 
$$\left(\frac{5^{n-1}}{6^{n-1}}\right) + \left(\frac{5^n}{6^n}\right)\left(\frac{1}{6}\right)$$
 B.  $\left(\frac{5^n}{6^n}\right) + \left(\frac{5^{n-1}}{6^{n-1}}\right)\left(\frac{1}{6}\right)$   
C.  $\left(\frac{5^n}{6^n}\right) + n\left(\frac{5^{n-1}}{6^{n-1}}\right)\left(\frac{1}{6}\right)$  D.  $\left(\frac{5^n}{6^n}\right) + n\left(\frac{5^{n-1}}{6^{n-1}}\right)\left(\frac{1}{6^2}\right)$ 

- 17. Let  $\vec{a} = 6\vec{i} - 3\vec{j} - 6\vec{k}$  and  $\vec{d} = \vec{i} + \vec{j} + \vec{k}$ . Suppose that perpendicular to  $\vec{d}$ . Then  $\vec{c}$  is  $\vec{a} = \vec{b} + \vec{c}$  where  $\vec{b}$  is parallel to  $\vec{d}$  and  $\vec{c}$  is
- A.  $5\vec{i}-4\vec{j}-\vec{k}$
- B.  $7\vec{i}-2\vec{j}-5\vec{k}$
- 0  $4\vec{i}-5\vec{j}+\vec{k}$
- D.  $3\vec{i}+6\vec{j}-9\vec{k}$
- 18 If  $\log_{(3x-1)}(x-2) = \log_{(9x^2-6x+1)}(2x^2-10x-2)$ , x equals then
- A.  $9 \sqrt{15}$
- B.  $3+\sqrt{15}$
- C.  $2+\sqrt{5}$
- D.  $6-\sqrt{5}$
- 19. Suppose a, b, c are positive integers such  $2^{a} + 4^{b} + 8^{c} = 328$ . Then  $\frac{a + 2b + 3c}{2}$  is equal to
- 0010
- 0
- D.
- 20. of the incircle of such a triangle is The sides of a right-angled triangle are integers. The length of one of the sides is 12. The largest possible radius

0

D. B

### PHYSICS

- 21. such a way that it slides off the other edge, 1 m away, after A small box resting on one edge of the table is struck in box and the table 2 seconds. The coefficient of kinetic friction between the
- must be less than 0.05
- B must be exactly zero
- 0 must be more than 0.05
- must be exactly 0.05
- 22. Carbon-11 decays to boron-11 according to the following formula.

$$_{6}^{11}C \rightarrow _{5}^{11}B + e^{+} + \nu_{e} + 0.96 \text{ MeV}$$

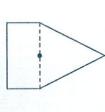
produced between time t = 0 and  $t = 2t_0$  will be nearly with the environment. At t=0 we have 1  $\mu g$  of  ${}_{6}^{12}C$ that the neutrinos  $(\nu_e)$  are massless and do not interact annihilate each other almost immediately. Also assume combine with free electrons in the atmosphere and Assume that positrons  $(e^+)$  produced in the decay If the half-life of the decay process is  $t_0$ , the net energy

- $8 \times 10^{18} \, \text{MeV}$
- B.  $8 \times 10^{16} \, \text{MeV}$
- $4 \times 10^{18} \,\mathrm{MeV}$
- D.  $4 \times 10^{16} \,\mathrm{MeV}$

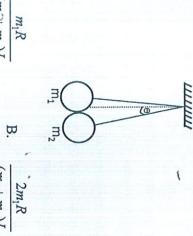
23. of mass of the composite body is located at the midpoint of different materials, one shaped like an isosceles triangle Two uniform plates of the same thickness and area but of triangle to that of the rectangle is their common side, the ratio between masses of the and the other shaped like a rectangle are joined together to form a composite body as shown in the figure. If the centre

25.

respect to its axis of symmetry is spinning counter A horizontal disk of moment of inertia 4.25 kg-m<sup>2</sup> with



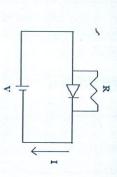
- O > 3:4 1:1
- D B 4:3 2:1
- 24. makes with the vertical is approximately shown in the figure  $(R \ll L)$ . The angle,  $\theta$  which mass  $m_2$ Two spherical objects each of radii R and masses  $m_1$  and  $m_2$  are suspended using two strings of equal length L as

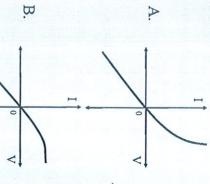


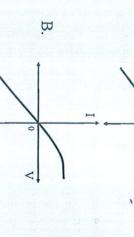
- 0 A  $(m_1 + m_2)L$  $(m_1+m_2)L$  $2m_2R$ 
  - $(m_1+m_2)L$
- D
- $(m_1+m_2)L$  $m_2R$

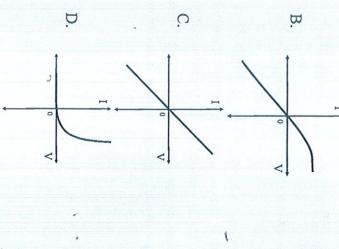
- viewed from above. A second disk of moment of inertia clockwise at 15 revolutions per second about its axis, as clockwise at 25 revolutions per second as viewed from 8 about their axis of symmetry. The new angular velocity of first disk. The two disks stick together and rotate as one above about the same axis and is dropped on top of the 1.80 kg-m<sup>2</sup> with respect to its axis of symmetry is spinning 0 the system as viewed from above is close to certain speed. If 5.25 seconds later he hears the ball hitting throws a ball in the vertically upward direction with a A boy is standing on top of a tower of height 85 m and 3 revolutions/second and counter clockwise. 3 revolutions/second and clockwise 18 revolutions/second and counter clockwise 18 revolutions/second and clockwise.
- 26. ball is (take  $g = 10 \text{ m/s}^2$ , speed of sound in air = 340 m/s) the ground, then the speed with which the boy threw the
- 6 m/s
- B 8 m/s
- 10 m/s
- D 12 m/s

27. For a diode connected in parallel with a resistor, which is the most likely current (I) – voltage (V) characteristic?





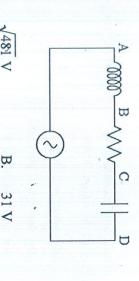




- 28. A beam of monoenergetic electrons, which have been the fringe width interference pattern in a Young's Double Slit experiment. accelerated from rest by a potential U, is used to form an The electrons are now accelerated by potential 4 U. Then
- remains the same.
- B. is half the original fringe width.
- 0 is twice the original fringe width.
- is one-fourth the original fringe width.
- 29. component of Earth's magnetic field is 30 micro Tesla) center of the circle will be reduced to zero? (Horizontal of the angular speed a, the effective magnetic field at the aligned along the magnetic axis of the earth. At what value vertical circle of radius R = 1 mm. The axis of the circle is A point charge Q (=  $3 \times 10^{-12}$  C) rotates uniformly in a
- 1011 rad/s
- **B** 10° rad/s
- 0 10<sup>13</sup> rad/s
- D. 10' rad/s
- 30. A closed bottle containing water at 30 °C is open on the surface of the moon. Then
- the water will boil.
- **B**. the water will come out as a spherical ball.
- 0 the water will freeze.
- the water will decompose into hydrogen and oxygen.

12

- A simple pendulum of length l is made to oscillate with an amplitude of 45 degrees. The acceleration due to gravity is g. Let  $T_0 = 2\pi \sqrt{l/g}$ . The time period of oscillation of this pendulum will be
- A  $T_0$  irrespective of the amplitude.
- 8 slightly less than  $T_0$ .
- 0 slightly more than  $T_0$ .
- D. dependent on whether it swings in a plane aligned with the north-south or east-west directions.
- 32. circuit below reads 36 V. If it is connected between A and An ac voltmeter connected between points A and B in the between B and D is 25 V. What will the voltmeter read C, the reading is 39 V. The reading when it is connected generates a pure ac.) voltmeter reads true rms voltage values and that the source when it is connected between A and D? (Assume that the



√481 V

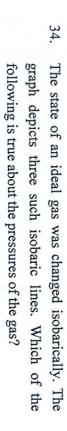
0

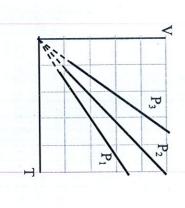
61 V

A.

- D.

- 33. A donor atom in a semiconductor has a loosely bound electron. The orbit of this electron is considerably affected of the hydrogen atom is 0.53Å) by the semiconductor material but behaves in many ways mass of the free electron) and the space in which it moves the electron has an effective mass of  $0.07m_e$ , (where  $m_e$  is lowermost energy orbit will be close to (The Bohr radius has a permittivity  $13\varepsilon_0$ , then the radius of the electron's like an electron orbiting a hydrogen nucleus. Given that
- 0.53 Å
- **B**. 243 Å
- 10 Å
- D. 100 Å





- $P_1 = P_2 = P_3$
- B P<sub>1</sub>>P<sub>2</sub>>P<sub>3</sub>
- $P_1 < P_2 < P_3$
- D  $P_1/P_2 = P_3/P$

- √3361 V

A metallic ring of radius a and resistance R is held fixed whose magnitude is  $B_0 \sin(\omega t)$ . Neglect gravity. Then, with its axis along a spatially uniform magnetic field

35.

- the current in the ring oscillates with a frequency
- the Joule heating loss in the ring is proportional
- 0 proportional to  $B_0^2$ . the force per unit length on the ring will be
- D. the net force on the ring is non-zero.
- 36. its mass M and the speed of light c as  $A = G^{\alpha}M^{\beta}c^{\gamma}$ . Here The dimensions of the area A of a black hole can be written in terms of the universal gravitational constant G,
- $\alpha = -2$ ,  $\beta = -2$ , and  $\gamma = 4$
- B.  $\alpha = 2$ ,  $\beta = 2$ , and  $\gamma = -4$
- $\alpha = 3$ ,  $\beta = 3$ , and  $\gamma = -2$
- D.  $\alpha = -3$ ,  $\beta = -3$ , and  $\gamma = 2$
- 37. A 160 watt infrared source is radiating light of wavelength distance of 1.8 m is of the order of 50000 Å uniformly in all directions. The photon flux at a
- A.  $10 \text{ m}^{-2} \text{ s}^{-1}$
- B.  $10^{10} \,\mathrm{m}^{-2} \,\mathrm{s}^{-1}$
- $10^{15} \text{ m}^{-2} \text{ s}^{-1}$
- D.  $10^{20} \,\mathrm{m}^{-2} \mathrm{s}^{-1}$

- 38. A wire bent in the shape of a regular n - polygonal loop the magnetic field at the centre of the loop is given by distance of a given segment and R be the distance of a vertex both from the centre of the loop. The magnitude of carries a steady current I. Let I be the perpendicular
- $\frac{n\mu_0 I}{2\pi l}\sin(\pi/n)$
- В.  $\frac{n\mu_0 I}{2\pi R}\sin(\pi/n)$
- 0  $\frac{n\mu_0 I}{2\pi l} \cos(\pi/n)$
- D.  $\frac{n\mu_0I}{2\pi R}\cos(\pi/n)$
- 39. by 100 times. This could imply a decibel level rise from The intensity of sound during the festival season increased
- 20 to 120 dB
- B. 70 to 72 dB
- 100 to 10000 dB
- D. 80 to 100 dB
- 40. One end of a slack wire (Young's modulus Y, length L and the wire becomes taut? horizontal plane. The block is set in motion with a speed v. other end to a block (mass m) which rests on a smooth cross-sectional area A) is clamped to a rigid wall and the What is the maximum distance the block will travel after
- $V\sqrt{\frac{mL}{AY}}$
- Β.  $V\sqrt{\frac{2mL}{AY}}$
- D.  $L\sqrt{\frac{m\nu}{AY}}$

## CHEMISTRY

- order The Lewis acid strength of BBr<sub>3</sub>, BCl<sub>3</sub> and BF<sub>3</sub> is in the
- BBr3<BCl3<BF3
- ₩. BCl3<BF3<BBr3
- 0 BF3<BCl3<BBr3
- D BBr3<BF3<BCl3
- 42. O<sup>2-</sup> is isoelectronic with
- $Zn^{2+}$
- B.

- 0
- D Ni<sup>2+</sup>
- 43. in methane, ammonia and water are respectively, closest to The H-C-H, H-N-H, and H-O-H bond angles (in degrees)
- 109.5, 104.5, 107.1
- B 109.5, 107.1, 104.5
- 104.5, 107.1, 109.5
- D. 107.1, 104.5, 109.5
- 44. which the oxidation state of Mn is with potassium permanganate produces a compound in In alkaline medium, the reaction of hydrogen peroxide
- ₿. +2
- 0 #3

- +4

- 45. The rate constant of a chemical reaction at a very high temperature will approach
- Arrhenius frequency factor divided by the ideal gas constant
- B activation energy
- 0 Arrhenius frequency factor
- activation energy divided by the ideal gas constant
- 46. The standard reduction potentials (in V) of a few metal ion/metal electrodes are given below.

follows the order  $Ag^{\dagger}/Ag = +0.8$ . The reducing strength of the metals  $Cr^{3+}/Cr = -0.74$ ;  $Cu^{2+}/Cu = +0.34$ ;  $Pb^{2+}/Pb = -0.13;$ 

- Ag>Cu>Pb>Cr
- B Cr > Pb > Cu > Ag
- Pb > Cr > Ag > Cu
- Cr > Ag > Cu > Pb
- 47. activity? Which of the following molecules can exhibit optical
- 1-bromopropane
- 2-bromobutane

Ä

- 3-bromopentane
- D. bromocyclohexane

48. The structure of the polymer obtained by the following reaction is





- 49. and (CH<sub>3</sub>)<sub>3</sub>CCl in ethanol is The major product of the reaction between CH<sub>3</sub>CH<sub>2</sub>ONa
- CH3CH2OC(CH3)3
- B CH<sub>2</sub>=C(CH<sub>3</sub>)<sub>2</sub>
- CH<sub>3</sub>CH<sub>2</sub>C(CH<sub>3</sub>)<sub>3</sub>
- D. CH3CH=CHCH3
- 50. solution containing Al3+, Cu2+, Pb2+ and Ni2+, a precipitate is formed which consists of When H<sub>2</sub>S gas is passed through a hot acidic aqueous
- CuS and Al2S3
- B.
- 0 CuS and NiS
- PbS and NiS
- PbS and CuS
- D

- 51. difference between the 1st and 2nd ionization energies is The electronic configuration of an element with the largest
- $1s^2 2s^2 2p^6 3s^1$
- $1s^2 2s^2 2p^6 3s^2$
- D.  $1s^2 2s^2 2p^1$
- 52. hybridized states follows The order of electronegativity of carbon in sp,  $sp^2$  and  $sp^3$
- $sp > sp^2 > sp^3$
- $sp^3 > sp^2 > sp$
- $sp > sp^3 > sp^2$
- D.  $sp^2 > sp > sp^3$
- 53. The most abundant transition metal in human body is
- copper
- zinc
- D. manganese
- 54. The molar conductivities of HCl, NaCl, CH3COOH, and CH<sub>3</sub>COONa at infinite dilution follow the order
- HCl > CH3COOH > NaCl > CH3COONa
- B. CH<sub>3</sub>COONa > HCl > NaCl > CH<sub>3</sub>COOH
- HCI > NaCl > CH3COOH > CH3COONa
- CH<sub>3</sub>COOH > CH<sub>3</sub>COONa > HCl > NaCl
- 55. where Z is The spin only magnetic moment of [ZCl<sub>4</sub>]<sup>2-</sup> is 3.87 BM
- A. Mn
- K
- D Cu

Co . ...

- 56. (are) If  $\alpha$ -D-glucose is dissolved in water and kept for a few hours, the major constituent(s) present in the solution is
- α-D-glucose
- B. mixture of  $\beta$ -D-glucose and open chain D-glucose
- 0 open chain D-glucose
- D. mixture of  $\alpha$ -D-glucose and  $\beta$ -D-glucose
- 57. HCOOH follows the order The pH of 1N aqueous solutions of HCl, CH<sub>3</sub>COOH and
- HCI > HCOOH > CH3COOH
- B HCI = HCOOH > CH<sub>3</sub>COOH
- CH<sub>3</sub>COOH > HCOOH > HCI
- D. CH<sub>3</sub>COOH = HCOOH > HCI
- 58. The major product of the reaction

Products

is

- 0
- B V
- D

59. Reaction of aniline with NaNO2+dil. HCl at 0°C followed by reaction with CuCN yields

$$- \begin{array}{c} NH_2 \\ NH_2 \\$$

- B
- H
- D V
- 60. Schottky defect in a crystal arises due to
- creation of equal number of cation and anion vacancies
- Β. creation of unequal number of cation and anion vacancies
- 0 migration of cations to interstitial voids
- migration of anions to interstitial voids

D.

## BIOLOGY

- rejection of graft post organ transplantation by Immunosuppressive drugs like cyclosporin delay the
- inhibiting T cell infiltration
- 8 killing B cells
- 0 killing macrophages
- D killing dendritic cells
- 62. Which one of these substances will repress the lac operon?
- Arabinose
- 8 Glucose
- Lactose
- D. Tryptophan
- 63. Assume a spherical mammalian cell has a diameter of amino acids should it be comprised of? conformation has to stretch across the cell, how many 27 microns. If a polypeptide chain with alpha helical
- 18000
- B. 1800
- 27000
- D. 12000
- 64 bonds?
- Deoxy ribonucleic acid
- B.
- D.
- Which one of the following has phosphoric acid anhydride
- Ribonucleic acid
- dNTPs
- Phospholipids

- 65. correct? mutually helpful. Which of the following statement is antagonistic actions. But in certain cases their effects are The two components of autonomous nervous system have
- At rest, the control of heart beat is not by the vagus
- **B** During exercise the sympathetic control decreases
- 0 decreases During exercise the parasympathetic control
- D. Stimulation of sympathetic system results in constriction of the pupil
- 66. of encountering a stop codon? In a random DNA sequence, what is the lowest frequency
- 1 in 20

1 in 3

- 1 in 64
- **B**.
- D 1 in 10
- 67. individual are located on The two alleles that determine the blood group AB of an
- two different autosomes
- B the same autosome
- 0 two different sex chromosomes
- D. autosome one on sex chromosome and the other on an

- 68. incorporated in a plasmid In biotechnology applications, a selectable marker is
- to increase its copy number
- B to increase the transformation efficiency
- 0 to eliminate the non-transformants
- to increase the expression of the gene of interest
- 69. Spermatids are formed after the second meiotic division secondary spermatocytes is from secondary spermatocytes. The ploidy of the

0 3n

- D 4n
- 70. Phospholipids are formed by the esterification of
- A three ethanol molecules with three fatty acid molecules
- 8 one glycerol and two fatty acid-molecules
- 0 one glycerol and three fatty acid molecules
- D one ethylene glycol and two fatty acids molecules
- Given the fact that histone binds DNA, it should be rich in
- A arginine, lysine
- B
- 0 glutamate, aspartate
- isoleucine, leucine

- cysteine, methionine
- D

- 72. mRNA that codes for this polypeptide? Assume that would be the minimum number of nucleotides in the If molecular weight of a polypeptide is 15.3 kDa, what molecular weight of each amino acid is 90 Da.
- 510
- В.

663

- 0 123
- D. 170
- 73. molecules are converted into single stranded molecules Melting temperature for double stranded DNA is the melting temperature? temperature at which 50% of the double stranded Which one of the following DNA will have the highest
- A. DNA with 15% guanine
- **B**. DNA with 30% cytosine
- 0 DNA with 40% thymine
- DNA with 50% adenine
- 74. paired? Following are the types of immunoglobulin and their functions. Which one of the following is INCORRECTLY
- IgD: viral pathogen
- B. IgG: phagocytosis
- IgE: allergic reaction
- IgM: complement fixation
- 75. acids? Which one of the following can be used to detect amino
- Iodine vapour
- 8. Ninhydrin
- Ethidium bromide
- D. Bromophenol blue

- 76. Mutation in a single gene can lead to changes in multiple traits. This is an example of
- Heterotrophy
- **B** Co-dominance
- Penetrance
- D. Pleiotropy
- 77. Which one of the following is used to treat cancers?
- Albumin
- Cyclosporin A
- Antibodies
- D. Growth hormone
- 78. formation? Which of the following processes leads to DNA ladder
- A. Necrosis
- Plasmolysis
- Apoptosis
- Mitosis
- 79. co-enzyme? Co-enzymes are components of an enzyme complex which are necessary for its function. Which of these is a known
- Zinc
- В. Vitamin B<sub>12</sub>
- Chlorophyll
- D. Heme
- 80. The peptidoglycans of bacteria consist of
- sugars, D-amino acids and L-amino acids
- sugars and only D-amino acids
- sugars and only L-amino acids
- sugars and glycine

Let  $x = (\sqrt{50} + 7)^{1/3} - (\sqrt{50} - 7)^{1/3}$ . Then

MATHEMATICS

Two-Mark Questions

PART II

$$A. \quad x=2$$

- B x = 3
- x is a rational number, but not an integer
- x is an irrational number
- 82.

$$(1+x+x^2)^{2014} = a_0 + a_1 x + a_2 x^2 + a_3 x^3 + \dots + a_{4028} x^{4028},$$
 and let

$$A = a_0 - a_3 + a_6 - \cdots + a_{4026}$$

$$B = a_1 - a_4 + a_7 - \cdots - a_{4027},$$

$$C = a_2 - a_5 + a_8 - \dots + a_{4028}.$$

A. 
$$|A| = |B| > |C|$$

B. 
$$|A| = |B| < |C|$$

$$|A| = |C| > |B|$$

). 
$$|A| = |C| < |B|$$

- 83. A mirror in the first quadrant is in the shape of a hyperbola whose equation is xy = 1. A light source in the second the slope of the incident beam is point (2, 1/2). If the reflected ray is parallel to the y-axis, quadrant emits-a beam of light that hits the mirror at the
- 8 15 8 13
  - **B**.
- D.

84. Let

$$C(\theta) = \sum_{n=0}^{\infty} \frac{\cos(n\theta)}{n!}.$$

Which of the following statements is FALSE?

- $C(0) \cdot C(\pi) = 1$
- B.  $C(0) + C(\pi) > 2$
- $C(\theta) > 0$  for all  $\theta \in \mathbb{R}$
- $C'(\theta) \neq 0$  for all  $\theta \in \mathbb{R}$
- 85. Let a > 0 be a real number. Then the limit

$$\lim_{x \to 2} \frac{a^x + a^{3-x} - (a^2 + a)}{a^{3-x} - a^{x/2}}$$

- $2\log a$
- 0
- $\frac{a^2+a}{2}$ 
  - D.
- $\frac{2}{3}(1-a)$

- 86. Let  $f(x) = \alpha x^2 - 2 + \frac{1}{x}$  where  $\alpha$  is a real constant. The smallest  $\alpha$  for which  $f(x) \ge 0$  for all x > 0 is
- 33 22
- B
- 0
- D 3 25
- 87. Let  $f: \mathbb{R} \to \mathbb{R}$  be a continuous function satisfying

$$f(x) + \int_{0}^{x} tf(t) dt + x^{2} = 0,$$

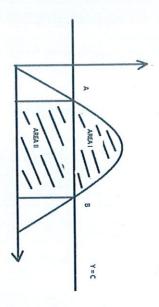
for all  $x \in \mathbb{R}$ . Then

- $\lim_{x\to\infty} f(x) = 2$
- $\lim_{x\to -\infty} f(x) = -2$

B

- 0 x -axis f(x) has more than one point in common with the
- D. f(x) is an odd function

The figure shows a portion of the graph  $y = 2x - 4x^3$ . The line y = c is such that the areas of the regions marked I and II are equal. If a, b are the x-coordinates of A, B respectively, then a + b equals



B. 
$$\frac{3}{\sqrt{7}}$$

89. Let  $X_n = \{1,2,3,...,n\}$  and let a subset A of  $X_n$  be chosen so that every pair of elements of A differ by at least 3. (For example, if n=5, A can be  $\emptyset$ ,  $\{2\}$  or  $\{1,5\}$  among others). When n=10, let the probability that  $1 \in A$  be p and let the probability that  $2 \in A$  be q. Then

A. 
$$p > q$$
 and  $p - q = \frac{1}{6}$ 

B. 
$$p < q \text{ and } q - p = \frac{1}{6}$$

C. 
$$p > q \text{ and } p - q = \frac{1}{10}$$

D. 
$$p < q \text{ and } q - p = \frac{1}{10}$$

# 90. The remainder when the determinant

$\begin{array}{ccccc} 2014^{2014} & 2015^{2015} & 2016^{2016} \\ 2017^{2017} & 2018^{2018} & 2019^{2019} \\ 2020^{2020} & 2021^{2021} & 2022^{2022} \end{array}$			
$2015^{2015}$ $2018^{2018}$ $2021^{2021}$	20202020	20172017	2014 <sup>2014</sup>
	20212021		2015 <sup>2015</sup>
	20222022	20192019	

is divided by 5 is

0

A cubical vessel has opaque walls. An observer (dark circle in figure below) is located such that she can see only corner C? Refractive index of water is 1.33. placed at the bottom at a distance of 10 cm from the should water be poured so that she can see an object the wall CD but not the bottom. Nearly to what height



- 0 27 cm 10 cm
- D. B. 16 cm

45 cm

92. perpendicular tangents AB, BC, CD, DA are I1, I2, I3 and its geometrical center is given by circle). The distance of the center of mass of the disc from (of mass M and radius R) about four mutually The moments of inertia of a non-uniform circular disc  $I_{4}$ , respectively (the square ABCD circumscribes the

A. 
$$\frac{1}{4MR}\sqrt{(I_1-I_3)^2+(I_2-I_4)^2}$$

B. 
$$\frac{1}{12MR}\sqrt{(I_1-I_3)^2+(I_2-I_4)^2}$$

C. 
$$\frac{1}{3MR}\sqrt{(I_1-I_2)^2+(I_3-I_4)^2}$$

D. 
$$\frac{1}{2MR}\sqrt{(I_1+I_3)^2+(I_2+I_4)^2}$$

93. when the temperature is 25 °C. The track is constrained A horizontal steel railroad track has a length of 100 m  $2 \times 10^{11} \text{ Pa}$ is  $1.1 \times 10^{-5}$  oC and the Young's modulus of steel is (Note: the linear coefficient of thermal expansion for steel hot summer day, when the temperature is 40 °C, is from expanding or bending. The stress on the track on a

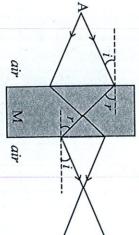
 $6.6 \times 10^7 \text{ Pa}$ 

₿.  $8.8 \times 10^7 \, \text{Pa}$ 

 $3.3 \times 10^7 Pa$ 

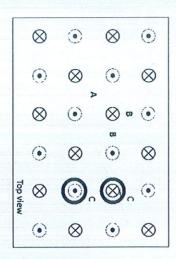
D.  $5.5 \times 10^7 \text{Pa}$ 

94. emerge from the other side as shown. The angles i and rare incident on a rectangular block of material M and possible are angles of incidence and refraction when the wave Electromagnetic waves emanating from a point A (in air) travels from air to the medium. Such paths for the rays are



- A. equal to zero. if the material has a refractive index very nearly
- **B**. only with gamma rays with a wavelength smaller than the atomic nuclei of the material
- 0 if the material has a refractive index less than zero.
- than the speed of light in vacuum. only if the wave travels in M with a speed faster

- 95. Two small metal balls of different mass  $m_1$  and  $m_2$  are connected by strings of equal length to a fixed point. When the balls are given equal charges, the angles that the two strings make with the vertical are 30° and 60°, respectively. The ratio  $m_1/m_2$  is close to
- A. 1.7
- B. 3.0
- C. 0.58
- D. 2.0
- 96. Consider the regular array of vertical identical current carrying wires (with direction of current flow as indicated in the figure below) protruding through a horizontal table. If we scatter some diamagnetic particles on the table, they are likely to accumulate

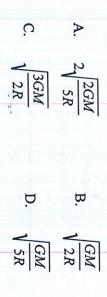


- A. around regions such as A.
- B. around regions such as B.
- C. in circular regions around individual wires such as C.
- D. uniformly everywhere.

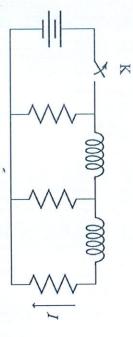
97. The distance between the vertex and the center of mass of a uniform solid planar circular segment of angular size  $\theta$  and radius R is given by



- A.  $\frac{4}{3}R\frac{\sin(\theta/2)}{\theta}$
- B.  $R \frac{\sin(\theta/2)}{\theta}$
- C.  $\frac{4}{3}R\cos\left(\frac{\theta}{2}\right)$
- D.  $\frac{2}{3}R\cos(\theta)$
- 98. An object is propelled vertically to a maximum height of 4R from the surface of a planet of radius R and mass M. The speed of object when it returns to the surface of the planet is



99. switched on for a long time. The currents through the three resistance on the right is I after the key K has been In the circuit shown below, all the inductors (assumed key is switched off are resistors (in order, from left to right) immediately after the ideal) and resistors are identical. The current through the

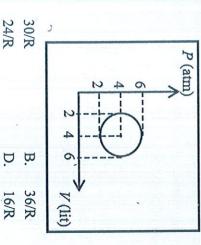


21 upwards, I downwards and I downwards.

A

B.

- 21 downwards, I downwards and I downwards.
- 0 I downwards, I downwards and I downwards.
- 0, I downwards and I downwards.
- 100. attained in this process is close to 4 lit as shown in the diagram. The maximum temperature



An ideal gas undergoes a circular cycle centered at 4 atm.

38

0

A.

## CHEMISTRY

101. For the reaction  $N_2 + 3X_2 \rightarrow 2NX_3$  where X = F, Cl and NCl<sub>3</sub> in kJ mol<sup>-1</sup>, respectively, are closest to and  $N=N=941 \text{ kJ mol}^{-1}$ ), the heats of formation of  $NF_3$  $N-F = 272 \text{ kJ mol}^{-1}$ ,  $Cl-Cl = 242 \text{ kJ mol}^{-1}$ ,  $N-Cl = 200 \text{ kJ mol}^{-1}$ (the average bond energies are  $F-F = 155 \text{ kJ mol}^{-1}$ 

-226 and +467

В. +226 and -467

-151 and +311

D. +151 and -311

102. The equilibrium constants for the reactions X = 2Y and are the same, the ratio  $K_1/K_2$  is concentrations and the degree of dissociation of X and Z Z = P + Q are  $K_1$  and  $K_2$ , respectively. If the initial

0.5

D.

103. The geometry and the number of unpaired electron(s) of [MnBr<sub>4</sub>]<sup>2-</sup>, respectively, are

tetrahedral and 1

В. square planar and 1

tetrahedral and 5 D. square planar and 5

- 104. The standard cell potential for Zn|Zn<sup>2+</sup>||Cu<sup>2+</sup>|Cu is 1.10 V. is closest to When the cell is completely discharged, log [Zn<sup>2+</sup>]/[Cu<sup>2+</sup>] 37.3 В. 0.026

18.7

D.

0.052

105. In the reaction

x, y and z are

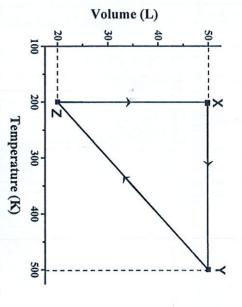
- x = Mg, dry ether;  $y = CH_3Cl$ ;  $z = H_2O$
- x = Mg, dry methanol;  $y = CO_2$ ; z = dil. HCl

B.

- 0 x = Mg, dry ether;  $y = CO_2$ ; z = dil. HCl
- x = Mg, dry methanol;  $y = CH_3Cl$ ;  $z = H_2O$
- 106. An organic compound having molecular formula C<sub>2</sub>H<sub>6</sub>O oxygen. The molecular formula of the compound X is which contains 40% carbon, 6.7% hydrogen and 53.3% undergoes oxidation with K2Cr2O7/H2SO4 to produce X
- CH<sub>2</sub>O
- B. C2H4O2
- C2H40
- D.  $C_2H_6O_2$
- 107. The maximum number of cyclic isomers (positional and optical) of a compound having molecular formula C3H2Cl.
- 8

- D

The volume vs. temperature graph of 1 mole of an ideal gas is given below



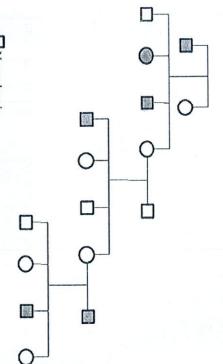
respectively, are The pressure of the gas (in atm) at X, Y and Z,

- 0.328, 0.820, 0.820 D. 3.28, 8.20, 3.28
- 0.238, 0.280, 0.280 32.8, 0.280, 82.0
- 109. MnO2 when fused with KOH and oxidized in air gives a and MnO2. The compounds X and Y, respectively, are disproportionation to give an intense purple compound Y dark green compound X. In acidic solution, X undergoes
- K<sub>2</sub>MnO<sub>4</sub> and KMnO<sub>4</sub> B. Mn2O7 and KMnO4
- K<sub>2</sub>MnO<sub>4</sub> and Mn<sub>2</sub>O<sub>7</sub> D. KMnO<sub>4</sub> and K<sub>2</sub>MnO<sub>4</sub>
- 110. A metal (X) dissolves both in dilute HCl and dilute NaOH produced by adding NH4Cl to the NaOH solution of X to liberate H<sub>2</sub>. Addition of NH<sub>4</sub>Cl and excess NH<sub>4</sub>OH to an The species X and Y, respectively, are HCl solution of X produces Y as a precipitate. Y is also
- Zn and Zn(OH)2 В. Al and Al(OH)3
- Zn and Na<sub>2</sub>ZnO<sub>2</sub> D. Al and NaAlO2

## BIOLOGY

- 111. How many bands are seen when immunoglobulin G molecules are analysed on a sodium dodecyl sulphatepolyacrylamide gel electrophoresis (SDS-PAGE) under reducing conditions?
- A.
- B
- 0
- D
- 112. In a mixed culture of slow and fast growing bacteria, penicillin will
- kill the fast growing bacteria more than the slow growing
- B growing kill slow growing bacteria more than the fast
- 0 kill both the fast and slow growing bacteria equally
- D. will not kill bacteria at all

Consider the following pedigree over four generations and haemophilia. mark the correct answer below about the inheritance of

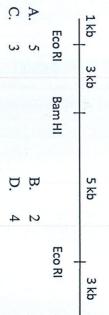


- ☐ Normal male
- Haemophilic male
- ONormal female
- Haemophilic female
- Haemophilia is X-linked dominant
- B Haemophilia is autosomal dominant
- Haemophilia is X-linked recessive
- Haemophilia is Y-linked dominant
- 114. A person has 400 million alveoli per lung with an average of that person is closest to alveoli are spherical in shape, the total respiratory surface radius of 0.1 mm for each alveolus. Considering the
- 500 mm<sup>2</sup>
- **B** 200 mm<sup>2</sup>
- $100 \text{ mm}^2$
- D. 1000 mm<sup>2</sup>

42

- is cultured in a medium containing a trace amount of radioactively labeled thymidine for one hour. The cells are then transferred to regular (unlabelled) medium. After 24 hrs of growth in regular media
- fast dividing cells will have maximum radioactivity
- B. slow dividing cells will have maximum radioactivity
- C. both will have same amount of radioactivity
- D. there will be no radioactivity in either types of cells
- 116. If a double stranded DNA has 15% cytosine, what is the % of adenine in the DNA?
- A. 15%
- B. 70%
- C. 35 %
- D. 30%
- 117. The mitochondrial inner membrane consists of a number of infoldings called cristae. The increased surface area due to cristae helps in:
- Increasing the volume of mitochondria
- B. Incorporating more of the protein complexes essential for electron transport chain
- C. Changing the pH
- D. Increasing diffusion of ions

- 18. The activity of a certain protein is dependent on its phosphorylation. A mutation in its gene changed a single amino acid which affected the function of the molecule. Which amino acid change is most likely to account for this observation?
- Tyrosine to Tryptophan
- B. Lysine to valine
- C. Leucine to isoleucine
- D. Valine to alanine
- 119. Consider the linear double stranded DNA shown below. The restriction enzyme sites and the lengths demarcated are shown. This DNA is completely digested with both *Eco*RI and *Bam*HI restriction enzymes. If the product is analyzed by gel electrophoresis, how many distinct bands would be observed?



- 120. Enzyme X catalyzes hydrolysis of GTP into GDP. The GTP-bound form of X transmits a signal that leads to cell proliferation. The GDP-bound form does not transmit any such signal. Mutations in X are found in many cancers. Which of the following alterations of X are most likely to contribute to cancer?
- . Mutations that increase the affinity of X for GDP.
- Mutations that decrease the affinity of X for GTP.
- Mutations that decrease the rate of GTP hydrolysis.
- Mutations that prevent expression of enzyme X.